

Directions: Beginning in the first cell marked #1, find the requested information. To advance in the circuit, hunt for your answer and mark that cell #2. Continue working in this manner until you complete the circuit. For all the following problems use a right hand Riemann sum with equal partitions.

<p><u>1</u>      Ans: <math>\int_3^5 \sqrt{x^3 + 1} dx</math></p> <p>Find a limit equal to <math>\int_0^4 (x^2 + 1) dx</math>.</p>	<p>_____      Ans: <math>\lim_{n \rightarrow \infty} \sum_{k=1}^n \ln \left( \frac{8}{n} k + 1 \right) \frac{4}{n}</math></p> <p>Find a limit equal to <math>\int_3^7 (x^2 - 8) dx</math>.</p>
<p>_____      Ans: <math>\int_2^4 (x^2 + 1) dx</math></p> <p>Find an integral expression equal to:</p> $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \left( \frac{2}{n} k \right)^3 + 3 \right) \frac{2}{n}.$	<p>_____      Ans: <math>\int_0^2 (x^3 + 2) dx</math></p> <p>Find an integral expression equal to:</p> $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \sqrt{\left( \frac{2}{n} k + 3 \right) + 1} \right) \frac{2}{n}.$

\_\_\_\_\_ Ans:  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \ln\left(\frac{4}{n}k + 1\right) \left(\frac{4}{n}\right)$

Find an integral expression equal to:

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \left( \frac{2}{n}k + 3 \right) + 1 \right) \frac{2}{n}$$

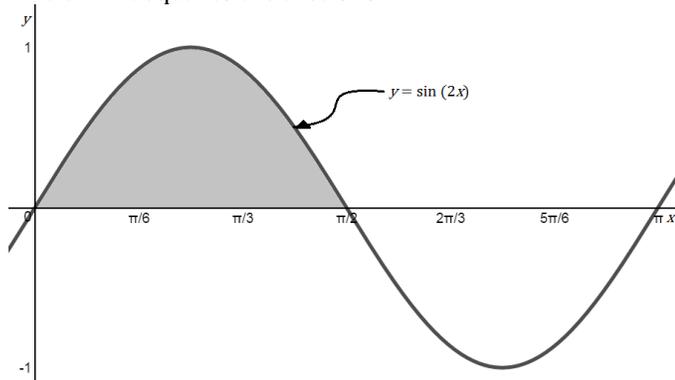
\_\_\_\_\_ Ans:  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \sqrt{\frac{16}{n}k + 9} \right) \frac{4}{n}$

Find an integral expression equal to:

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \left( \frac{2}{n}k \right)^2 + 3 \right) \frac{2}{n}$$

\_\_\_\_\_ Ans:  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \frac{16}{n^2}k^2 + \frac{24}{n}k + 1 \right) \frac{4}{n}$

Find a limit equal to the area shown.



\_\_\_\_\_ Ans:  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \frac{16}{n^2}k^2 + 1 \right) \frac{4}{n}$

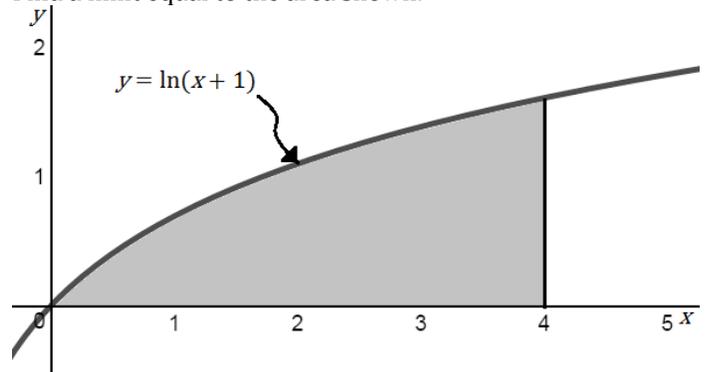
Find a limit equal to  $\int_0^{\pi/2} \cos(2x) dx$ .

\_\_\_\_\_ Ans:  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \cos\left(\frac{\pi}{n}k\right) \right) \frac{\pi}{2n}$

Find a limit equal to  $\int_3^7 \sqrt{4x-3} dx$ .

\_\_\_\_\_ Ans:  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \sqrt{\frac{4}{n}k + 2} \right) \frac{4}{n}$

Find a limit equal to the area shown.



\_\_\_\_\_ Ans:  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \sin\left(\frac{\pi}{n}k\right) \right) \frac{\pi}{2n}$

Find an integral expression equal to:

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \left( \frac{2}{n}k \right)^3 + 2 \right) \frac{2}{n}$$

\_\_\_\_\_ Ans:  $\int_3^5 (x+1) dx$

Find an integral expression equal to:

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \sqrt{\left( \frac{2}{n}k + 3 \right)^3 + 1} \right) \frac{2}{n}$$

\_\_\_\_\_ Ans:  $\int_3^5 \sqrt{x+1} dx$

Find an integral expression equal to:

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \left( \frac{2}{n}k + 2 \right)^2 + 1 \right) \frac{2}{n}$$

\_\_\_\_\_ Ans:  $\int_0^2 (x^2 + 3) dx$

Find an integral expression equal to:

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \sqrt{\left( \frac{2}{n}k + 3 \right)^2 + 1} \right) \frac{2}{n}$$

\_\_\_\_\_ Ans:  $\int_3^5 \sqrt{x^2 + 1} dx$

Find a limit equal to  $\int_1^5 \ln(2x - 1) dx$ .

\_\_\_\_\_ Ans:  $\int_0^2 (x^3 + 3) dx$

Find a limit equal to the area shown.

